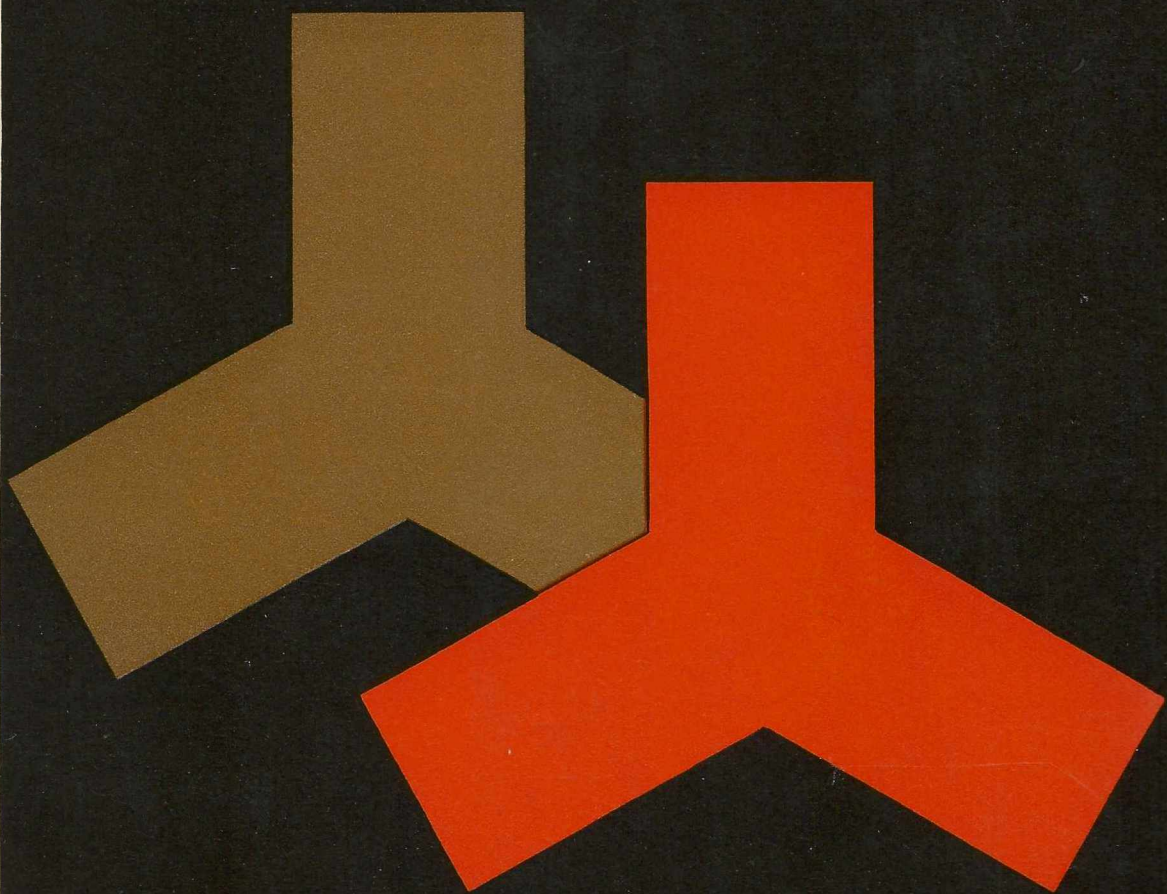


Combinatorial Problems and Exercises

by László Lovász



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Akadémiai Kiadó Budapest

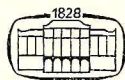
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by

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